

Name:

**MATH221**  
test #2, 10/27/16  
Sections 1.8–1.9, 2.1–2.3  
Total 100

Show all work legibly.

1. (20) Let  $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$ . Find  $A^{-1}$  if exists.

$$A^{-1} = .$$

2. (20) Let  $A = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$ . If  $B$  is a  $2 \times 3$  matrix so that  $AB = C = \begin{bmatrix} 6 & 1 & 2 \\ 3 & 4 & 5 \end{bmatrix}$ . Find  $B$ .

$B =$

3. (20) Let  $A = \begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix}$ . Identify all  $2 \times 3$  matrices  $X$  that solve  $AX = \begin{bmatrix} 4 & 5 & 6 \\ 4 & 5 & 6 \end{bmatrix}$ .

$X =$

4. (40) Let  $T : \mathbf{R}^2 \rightarrow \mathbf{R}^2$  be a linear transformation so that  $T(\mathbf{e}_1) = \mathbf{e}_2$ , and  $T(\mathbf{e}_2) = \mathbf{e}_1$ .
- (a) (10) Find  $A$  the standard matrix of the transformation.

$$A =$$

(b) (15) True or False?  $T$  is one-to-one.

Mark one and explain.

True       False

(c) (15) True or False?  $T$  is onto.

Mark one and explain.

True       False