

HW 1  
Answer Key

Section 2.2 # 6, 10 [a-d]  
Section 2.3 # 1, 9, 11

6

	A	B	
Product x	50%	40%	\$10/gal
Product y	20%	10%	\$21/gal
Requirements	$\geq 30\%$	$\geq 30\%$	

CORRECT MODEL  $\rightarrow$

minimize  $10x + 21y$

Subject to

$x + y = 100$

$.5x + .2y \geq 30$

$.4x + .1y \geq 30$

$x, y \geq 0$

a.) The constraints in a) are incorrect. To use the constraints given, you would also need  $x + y = 1$ . Furthermore, you must test all corner points to be sure of which minimizes  $10x + 21y$

b.)  $x = 0, y = 0$  does satisfy the constraints, but this model is also incorrect.

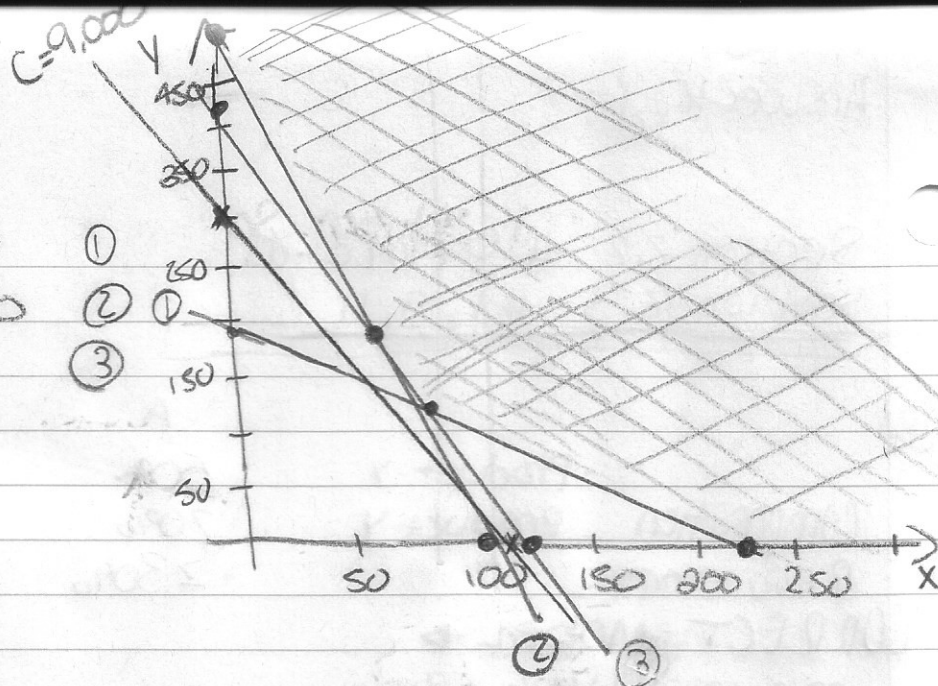
c.) See above

10

a)	A	B	C	Cost
Feed x	2/lb	5/lb	7/lb	80¢/lb
Feed y	3/lb	1/lb	2/lb	30¢/lb
Required	550	600	820	minimize

minimize  $80x + 30y$   
Subject to?

$$\begin{aligned} 2x + 3y &\geq 550 & \textcircled{1} \\ 5x + 1y &\geq 500 & \textcircled{2} \\ 7x + 2y &\geq 820 & \textcircled{3} \\ x, y &\geq 0 \end{aligned}$$



Try  $C = 9,000$

Cost line will intersect first with the corner at the intersection of  $\textcircled{1}$  and  $\textcircled{3}$

$$\begin{aligned} 2x + 3y &= 550 \\ 7x + 2y &= 820 \end{aligned}$$

$$\begin{aligned} -4x - 6y &= -1100 \\ 21x + 6y &= 2460 \\ 17x &= 1360 \end{aligned}$$

$$\boxed{\begin{aligned} x &= 80 \\ y &= 130 \end{aligned}}$$

$$b) -7/2 \leq -c_1/c_2 \leq -2/3$$

$$\boxed{2/3 \leq c_1/c_2 \leq 7/2}$$

$$\begin{aligned} c) \quad 2/3 &\leq c_1/30 \leq 7/2 \\ 20 &\leq c_1 \leq 105 \end{aligned}$$

$c_1$  can increase to 105 or 115 before the optimal point changes

The new optimal point would be at the intersection of  $\textcircled{2}$  and  $\textcircled{3}$

$$\boxed{\begin{aligned} x &= 60 \\ y &= 200 \end{aligned}}$$

d) The original solution satisfies this constraint.

$$x = 80$$

$$y = 130$$

$$x = 80 < 215$$

Section 2.3

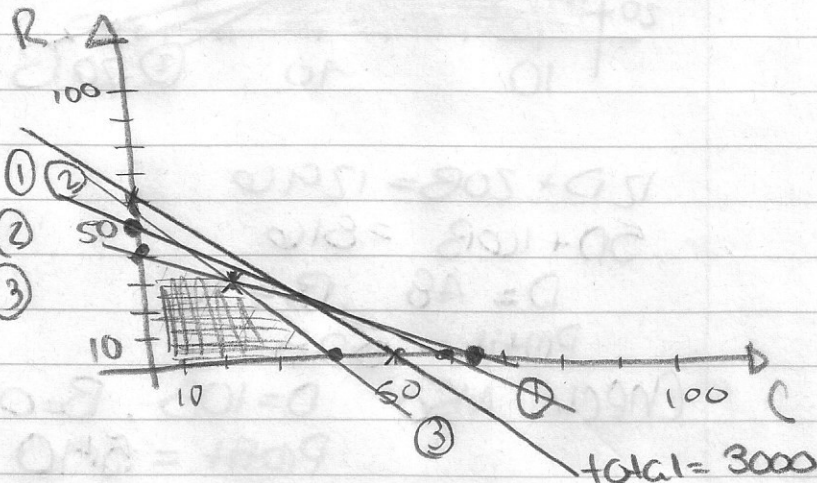
① Maximize  $50R + 60C$   
Subject to:

$$50R + 30C \leq 2000 \quad (1)$$

$$60R + 50C \leq 300 \quad (2)$$

$$30R + 50C \leq 200 \quad (3)$$

$$R, C \geq 0$$



consider: total = 3000

Will intersect the shaded region first at the intersection of (1) and (3)

$$50R + 30C = 2000$$

$$30R + 50C = 200$$

$$-18R - 30C = -1200$$

$$\hline 32R = 800$$

$$R = 25$$

$$\boxed{\begin{matrix} R = 25 \\ C = 25 \end{matrix}}$$

⑨ B = Box of Brownies

D = Dozen Bran Muffins

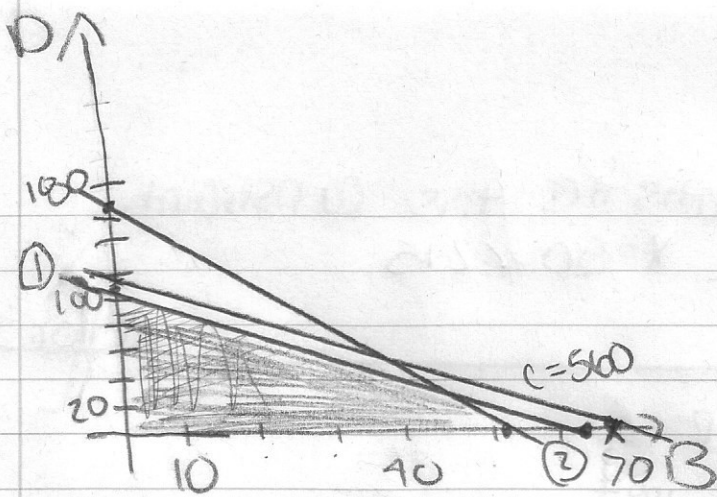
Maximize  $5D + 8B$

Subject to:

$$12D + 20B \leq 1296 \quad (1)$$

$$5D + 10B \leq 816 \quad (2)$$

$$D, B \geq 0$$



$$12D + 20B = 1296$$

$$5D + 10B = 810$$

$$D = 48, B = 36$$

$$\text{Profit} = 528$$

Check also  $D = 108, B = 0$

$$\text{Profit} = 540$$

$$\begin{aligned} D &= 108 \\ B &= 0 \end{aligned}$$

- ①① maximize  $8R + 60T + 45S$   
 Subject to:  $2R + 12T + 15S \leq 1500$   
 $R + 8T + 6S \leq 920$   
 $R, T, S \geq 0$