## MATH221 Fall 2018 Bonus Problems

- 1. (1pt) Assigned on: Solved on ?: by: Diae Mizon Let ABC be a triangle so that  $AB^2 + AC^2 = BC^2$ . True or False?  $\angle BAC = 90^{\circ}$ .
- 2. (1pt) Assigned on: Solved on: September 14, 2018 by: Greg Friedman Let  $\mathbf{x}, \mathbf{y} \in \mathbf{R}^2$ . Consider the set of vectors  $\{\mathbf{z} : \mathbf{z} = t\mathbf{x} + (1-t)\mathbf{y}, 0 \le t \le 1\}$ . Show that set Z is a segmet of staright line connecting  $\mathbf{x}$  and  $\mathbf{y}$ .
- 3. (1pt) Assigned on: September 27, 2018 Solved on: by: Let  $\{\mathbf{a}_1, \ldots, \mathbf{a}_n\}$  be a set of linearly independent vectors. True or False? If B is a matrix with linearly independent columns, the the vectors  $\{B\mathbf{a}_1, \ldots, B\mathbf{a}_n\}$  are linearly independent.
- 4. (1pt) Assigned on: October 9, 2018 Solved on: October 9, 2018 by: Lyeba Hameed Show that  $(AB)^T = B^T A^T$ . (Hint: Let  $B = [\mathbf{b}_1, \ldots, \mathbf{b}_n]$ . Consider the matrix  $B_1 = [\mathbf{b}_1, 0, \ldots, 0]$ . First show that  $(AB_1)^T = B_1^T A^T$ , then use that  $B = B_1 + B_2 + \ldots + B_n$ where  $B_i$  is a matrix with column *i* being  $\mathbf{b}_i$ , and all other columns being 0.)
- 5. (1pt) Assigned on: November 8, 2018 Solved on: by: Let A and B be two matrices so that rank  $A = \operatorname{rank} B$ . True or False? A and B are row equivalent.
- 6. (1pt) Assigned on: November 13, 2018 Solved on: by: Let A be a  $3 \times 3$  matrix. Show that the cofactor expansion across any row or across any column leads to the same result.
- 7. (1pt) Assigned on: November 13, 2018 Solved on: by: Show that det  $AB = \det A \det B$ .
- 8. (1pt) Assigned on: November 13, 2018 Solved on: by: Show that det  $A = \det A^T$ .
- 9. (1pt) Assigned on: November 29, 2018 Solved on: by: Prove that det A = 0 yields linear dependance of columns of A.