

1. Assigned: 180130, points: 1, solved by: Zachary Zhao on: 180205
Let $A = \{x : 0 \leq x \leq 1\}$, and $B = \{x : 0 < x < 1\}$. True or False? There is a bijection between A and B .

2. Assigned: 180130, points: 1, solved by: Lyranne Leoni on: 180201
Let $A = \mathbf{R}$, and $B = \{x : 0 < x < 1\}$. True or False? There is a bijection between A and B .

3. Assigned: 180201, points: 1, solved by: on:
Let T be a triangle. True or False? There is a family of segments I_α so that

$$\bigcup I_\alpha = T, \text{ and } I_\alpha \cap I_\beta = \emptyset \text{ if } \alpha \neq \beta.$$

4. Assigned: 180213, points: 1, solved by: on:
True or False? If $n \in \mathbf{N}$, then \sqrt{n} is either integer, or irrational.

5. Assigned: 180215, points: 1, solved by: on:
geometric mean \leq arithmetic mean

6. Assigned: 180222, points: 1, solved by: on:
A rabbit is hopping with an irrational step size α over a unit circle. A trap (interval) of length $\beta > 0$ is waiting for him. Show that the rabbit will be caught in the trap.

7. Assigned: 180413, points: 2, solved by: on:
True or False? $\sin n$ is dense in $[-1, 1]$.

8. Suggested by: Jeff Coleman, Assigned: 180503, points: 2, solved by: on:
Let $\{x_n\}$ be a sequence of positive real numbers such that $\lim_{n \rightarrow \infty} x_n = 1$. True or False? $\left\{x_n^{\frac{1}{n}}\right\}$ converges.