

Homework 4

1. Let $\{\mathbf{v}_1, \dots, \mathbf{v}_n\}$ be a set of linearly independent vectors in a vector space V , and $\mathbf{u} \in V$. True or False? If $\text{span } \{\mathbf{v}_1, \dots, \mathbf{v}_n\} \subset \text{span } \{\mathbf{v}_1, \dots, \mathbf{v}_n, \mathbf{u}\}$, then the vector set $\{\mathbf{v}_1, \dots, \mathbf{v}_n, \mathbf{u}\}$ is linearly independent.
2. Let A be an $n \times n$ Vandermonde matrix. Show that $\det A = \prod_{i>j} (x_i - x_j)$.