

## Homework 4

1. Let  $\{\mathbf{v}_1, \dots, \mathbf{v}_n\}$  be a set of linearly independent vectors in a vector space  $V$ , and  $\mathbf{u} \in V$ . True or False? If  $\text{span } \{\mathbf{v}_1, \dots, \mathbf{v}_n\} \subset \text{span } \{\mathbf{v}_1, \dots, \mathbf{v}_n, \mathbf{u}\}$ , then the vector set  $\{\mathbf{v}_1, \dots, \mathbf{v}_n, \mathbf{u}\}$  is linearly independent.
2. Let  $A$  be an  $n \times n$  Vandermonde matrix. Show that  $\det A = \prod_{i>j} (x_i - x_j)$ .